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A weighted voltage model predictive control method for a virtual synchronous generator with enhanced parameter robustness



Leilei Guo, Zhiye Xu, Nan Jin*, Yanyan Li and Wei Wang

Abstract

To address the problem of insufficient system inertia and improve the power quality of grid-connected inverters, and to enhance the stability of the power system, a method to control a virtual synchronous generator (VSG) output voltage based on model predictive control (MPC) is proposed. Parameters of the inductors, capacitors and other components of the VSG can vary as the temperature and current changes. Consequently the VSG output voltage and power control accuracy using the conventional MPC method may be reduced. In this paper, to improve the parameter robustness of the MPC method, a new weighted predictive capacitor voltage control method is proposed. Through detailed theoretical analysis, the principle of the proposed method to reduce the influence of parameter errors on voltage tracking accuracy is analyzed. Finally, the effectiveness and feasibility of the proposed method are verified by experimental tests using the Typhoon control hardware-in-the-loop experimental platform.

Keywords: Virtual synchronous generator, Model predictive control, Optimal voltage vector, Parameter error compensation

1 Introduction

The development of clean, efficient and renewable energy is one of society's top priorities, while electricity is the main way to use energy and is an indispensable part of people's lives and national development [1]. Distributed generation (DG), as an effective supplement to centralized power generation, is being increasingly widely used in power systems [2–4].

In order to ensure the quality of power supply for users while reducing the adverse effects when DGs are connected to the grid, the concept of the microgrid has been proposed. In most microgrids, the parallel operation of distributed and large power grids is achieved through inverters. Thus, how to effectively control the inverters so that the microgrid can be better connected to the large power grid is critical [5, 6]. There are many control

strategies for voltage control of microgrid inverters, including: (1) constant power (PQ), (2) constant voltage and constant frequency (V/f) [7], and (3) droop control [8]. However, these methods lack inertia provision and damping characteristics, and thus are not conducive to the stability of the system [9] and in severe cases, the system may even collapse. Therefore, these conditions need to be considered in the control process, resulting in a complicated control system.

By introducing the rotor mechanical equation and the stator electrical characteristic equation of the synchronous generator in the control, the virtual synchronous generator (VSG) can make the inverter exhibit the characteristics of the synchronous generator. The VSG provides inertia and damping, and helps maintain the stability of the power system. This makes the study the grid-connected inverter control method based on a VSG of significance [10, 11].

Much research has been conducted on the application of VSG control schemes. In [12], the method of using a

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VSG to improve the frequency stability of a photovoltaic microgrid is studied, where the VSG control emulates the inertial response and system damping by injecting power into the energy storage system. Reference [13] studies the VSG control of the grid-connected inverter in a microgrid. Using the VSG algorithm as the power outer loop, a voltage and current double closed-loop system is designed to improve stability. However, the above VSG controls are based on the PWM method, requiring the design of multiple proportional integral (PI) controllers which are difficult to design and tune.

In recent years, there has been increased interest in the application of model predictive control (MPC) technology in the field of power electronics [14-17], as it does not require the design of a PI controller and a PWM algorithm. In [16], an adaptive compensation algorithm based on inherent frequency is proposed to estimate the power grid voltage, and an MPC strategy is then designed using the estimated grid voltage to reduce current ripple. In [17], an improved MPC-based common-mode voltage (CMV) reduction method is proposed to reduce the CMV and eliminate the CMV spikes for two-level voltage source inverters. However, there has been limited research on the control method combining VSG and MPC. In [18], an improved finite-set MPC is proposed for the inner loop. This has a simple control structure, faster dynamic response, and enhanced control bandwidth and stability. In the outer control loop, a simplified VSG without a phase-locked loop is employed to realize active power sharing and inertia emulation. Nevertheless, the above MPC methods often assume that the inverter model used for prediction is consistent with the actual system. The parameter errors of the inverters, errors which affect system control performance, are not considered [19].

In [20], a new adaptive control scheme that uses the average switching frequency to adjust the parameter values of the predictive model online is presented. This control scheme can keep the average switching frequency within an acceptable operational margin, while improving the stability of the control system. In [21], the extended control vectors are adopted to improve the control precision, and an indirect reference vector strategy is developed to avoid the penalty of heavy computation time and increase robustness. In [22], a robust MPC method is proposed based on the current error. By studying the effects of parameter changes on the current error, two PI controllers are then adopted to extract accurate inductance and flux linkage parameters. However, the error compensations in [21, 22] require several PI controllers, which as we have said are difficult to design and tune. In addition there is a lack of detailed theoretical support.

In this paper, to achieve the control of VSG without using a PI controller and a PWM algorithm, and to enhance parameter robustness, a new weighted voltage MPC method for the VSG is proposed. The main improvements of this work over existing studies are:

- (1) Detailed theoretical analysis of the influence of parameter changes on the conventional MPC for the VSG is conducted to show its sensitivity to parameter errors.
- (2) A new weighted voltage MPC method is proposed for the VSG, which uses the weighted sum of the sampled voltage and the predicted one to predict the voltage at the next period.
- (3) A detailed theoretical analysis is carried out to show the influence of parameter changes on the proposed weighted voltage MPC method. This analysis verifies the enhanced robustness of the proposed method against parameter variations.
- (4) The outer-loop of the VSG, which generates the reference voltage for the proposed weighted voltage MPC method, is designed to control the active and reactive power, and to solve the problem of insufficient system inertia.
- (5) Compared to the conventional VSG control method, the proposed method can achieve direct output voltage predictive control without a PI controller and a PWM algorithm.
- (6) A PE-Expert4 and Typhoon-602 + based hardwarein-the-loop experimental study is carried out, which further verifies the feasibility and effectiveness of the proposed strategy.

2 VSG model and its control

The VSG enables grid-connected inverters to emulate the operating mechanism of synchronous generators, so they have the same operational mechanism and external characteristics as traditional synchronous generators. Such chararacteristics are: torque inertia, active power frequency modulation, and reactive power voltage regulation.

The topology of the inverter with an output LC filter is shown in Fig. 1, where the DC power supply and the three-phase inverter with the output LC filter can be equivalent to the VSG. The control block diagram of the VSG is shown in Fig. 2, which mainly includes the VSG model and its core control algorithm. The former emulates the electromagnetic relationship and mechanical movement of the synchronous generator, while the latter mainly adopts frequency and voltage regulation to realize active and reactive power control.

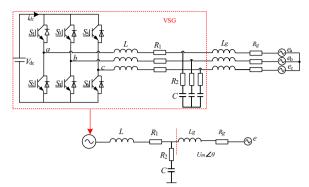


Fig. 1 Topological map of the inverter with output LC filter

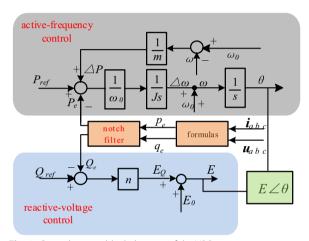


Fig. 2 Control system block diagram of the VSG

2.1 Active power frequency control

The active power frequency control of a VSG is by emulating the rotor equation of the synchronous generator. The second-order equation of the traditional synchronous generator is used for modeling [23]:

$$\begin{cases} J\omega_0 \frac{d\omega}{dt} = P_{\rm m} - P_{\rm e} - D_{\rm p}(\omega - \omega_0) \\ \frac{d\theta}{dt} = \omega \end{cases}$$
 (1)

where $P_{\rm m}$ and $P_{\rm e}$ are the mechanical and average power of the synchronous generator, respectively. J is the rotary inertia of the synchronous generator. $D_{\rm p}$ is the damping coefficient. ω and ω_0 are the angular frequencies of the synchronous generator and grid, respectively. θ is the rotation angle of the generator rotor relative to the a-phase stator winding. The virtual mechanical power of the VSG is calculated by:

$$P_{\rm m} = P_{\rm ref} + \Delta P = P_{\rm ref} + \frac{1}{\rm m}(\omega_0 - \omega) \tag{2}$$

where $P_{\rm ref}$ is the reference active power. ΔP is the output of the VSG frequency regulator. m is an active power adjustment factor which contains the damping coefficient $D_{\rm p}$. The instantaneous electromagnetic power p_e of the VSG is calculated by:

$$p_e = 1.5(u_{c\alpha}i_{\alpha} + u_{c\beta}i_{\beta}) \tag{3}$$

where i_{α} , i_{β} are the grid currents in the $\alpha\beta$ coordinate, and $u_{c\alpha}$, $u_{c\beta}$ are the voltages at the filter bus in the $\alpha\beta$ coordinate. The output average active power of the VSG $P_{\rm e}$ can be obtained through a notch filter to reduce power fluctuation [12], as:

$$P_{\rm e} = \frac{s^2 + \omega_{\rm m}^2}{s^2 + 2\delta\omega_{\rm m}s + \omega_{\rm m}^2} p_{\rm e} \tag{4}$$

where $\omega_{\rm m}$ is the harmonic angular frequency of the notch filter and δ is the quality factor.

It can be seen from the above formulas that J emulates the moment of inertia. This can reduce system frequency fluctuation after disturbances. The frequency returns to the rated value by adjusting $P_{\rm m}$ and $P_{\rm e}$. The difference between the VSG output angular frequency ω and the grid frequency ω_0 is used as feedback for the active power–frequency control to obtain the VSG output angular frequency ω , while the phase reference θ is obtained by integration of ω .

2.2 Reactive power voltage control

For the VSG reactive power voltage control, the control block diagram is shown in Fig. 2, where *E* is the reference voltage amplitude and consists of two parts:

$$E = E_0 + E_Q = E_0 + n(Q_{\text{ref}} - Q_e)$$
 (5)

where E_0 is the no-load EMF of the VSG. E_Q is the output voltage of the reactive power regulator. n is the reactive power adjustment factor. $Q_{\rm ref}$ is the reference reactive power, and $Q_{\rm e}$ is the output average reactive power of the VSG, obtained as:

$$Q_{\rm e} = \frac{s^2 + \omega_{\rm m}^2}{s^2 + 2\delta\omega_{\rm m}s + \omega_{\rm m}^2} 1.5 (u_{\rm c\beta}i_{\alpha} - u_{\rm c\alpha}i_{\beta})$$
 (6)

The reference voltage amplitude E and the angle θ obtained by the active power frequency control are combined to derive the reference voltage for the inner-loop voltage predictive control.

3 Voltage model predictive control for VSG

3.1 Principle of voltage model predictive control

The 2-level 3-phase inverter shown in Fig. 1 has 8 voltage vectors, as shown in Fig. 3. From Fig. 1, the dynamic vector equation can be expressed as:

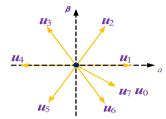


Fig. 3 The output voltage vectors

$$\begin{cases}
L \frac{d\mathbf{i}_{f\alpha\beta}}{dt} = \mathbf{u} - \mathbf{u}_{\text{C}\alpha\beta} - \mathbf{i}_{f\alpha\beta} R_1 \\
C \frac{d[\mathbf{u}_{c\alpha\beta} - R_2(i_{f\alpha\beta} - i_{\alpha\beta})]}{dt} = i_{f\alpha\beta} - i_{\alpha\beta}
\end{cases} (7)$$

where L is the output filter inductance of the inverter, and C is the filter capacitor. R_1 and R_2 are the parasitic resistances of the filter inductor and filter capacitor, respectively. $\boldsymbol{i}_{\text{f}\alpha\beta}$ and $\boldsymbol{i}_{\alpha\beta}$ are the current vectors flowing through the filter inductor L and the grid-side inductor L_g in the $\alpha\beta$ coordinate, respectively. \boldsymbol{u} is the output voltage vector of the inverter, and $\boldsymbol{u}_{c\alpha\beta}$ is the voltage vector at the filter bus. Equation (7) can be discretized as:

$$\begin{cases} \mathbf{i}_{f\alpha\beta}(k+1) = \frac{T_s}{L_f} \left[\mathbf{u}_{\alpha\beta}(k) - \mathbf{u}_{c\alpha\beta}(k) - \mathbf{i}_{f\alpha\beta} \cdot R_1 \right] + \mathbf{i}_{f\alpha\beta}(k) \\ \mathbf{u}_{c\alpha\beta}(k+1) = \frac{T_s}{C} \left[\mathbf{i}_{f\alpha\beta}(k+1) - \mathbf{i}_{\alpha\beta}(k) \right] + \mathbf{u}_{c\alpha\beta}(k) \\ + R_2 \left[\mathbf{i}_{f\alpha\beta}(k+1) - \mathbf{i}_{\alpha\beta}(k+1) - \mathbf{i}_{f\alpha\beta}(k) + \mathbf{i}_{\alpha\beta}(k) \right] \end{cases}$$
(8)

where T_s is the sampling period.

Assuming that $i_{\alpha\beta}(k) = i_{\alpha\beta}(k+1)$, the prediction functions of $i_{f\alpha\beta}$ and $u_{c\alpha\beta}$ can be obtained as:

$$\begin{cases}
\mathbf{i}_{\text{f}\alpha\beta}(k+1) = \frac{T_{\text{s}}}{L} \left[\mathbf{u}_{\alpha\beta}(k) - \mathbf{u}_{\text{c}\alpha\beta}(k) \right] - \frac{T_{\text{s}}}{L} \mathbf{i}_{\text{f}\alpha\beta}(k) \cdot R_{1} \\
+ \mathbf{i}_{\text{f}\alpha\beta}(k) \\
\mathbf{u}_{\text{c}\alpha\beta}(k+1) = \frac{T_{\text{s}}}{C} \left[\mathbf{i}_{\text{f}\alpha\beta}(k+1) - \mathbf{i}_{\alpha\beta}(k) \right] + \mathbf{u}_{\text{c}\alpha\beta}(k) \\
+ R_{2} \left[\mathbf{i}_{\text{f}\alpha\beta}(k+1) - \mathbf{i}_{\text{f}\alpha\beta}(k) \right]
\end{cases} \tag{9}$$

From (9), once the current $i_{\text{f}\alpha\beta}$ (k) and the capacitor voltage $u_{\text{c}\alpha\beta}$ (k) at the current time t_k are sampled, the inductor current $i_{\text{f}\alpha\beta}$ (k+1) at time t_{k+1} can be predicted. Then, by sampling the grid current $i_{\alpha\beta}$ (k), the voltage $u_{\text{c}\alpha\beta}$ (k+1) at time t_{k+1} can be further predicted. The cost function is constructed by sampling the reference voltage generated by the virtual synchronous control as:

$$g = |u_{\alpha}^* - u_{c\alpha}(k+1)| + |u_{\beta}^* - u_{c\beta}(k+1)|$$
 (10)

where u_{α}^* and u_{β}^* are the reference voltages, whereas $u_{c\alpha}$ (k+1) and $u_{c\beta}$ (k+1) are the predicted voltage values at the next sampling instant.

The voltage vectors corresponding to the eight switching states are sequentially substituted into (10). By comparing the cost functions, the optimal switch state corresponding to the voltage vector that minimizes the

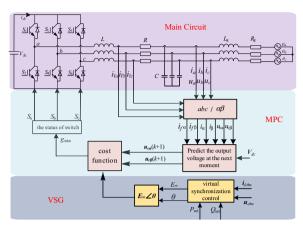


Fig. 4 VSG control block diagram based on voltage model predictive control

cost function is selected and applied in the next control period. The VSG control block diagram based on voltage predictive control is shown in Fig. 4.

3.2 Influence of parameter error on control performance

As the MPC strategy is a model-based control method, parameter changes can influence its control performance. Considering the temperature and current change during inverter operation, the actual values of the device parameters (filter inductance, filter capacitance, resistance, etc.) often deviate from their theoretical values. This deviation may affect the entire process of voltage predictive control. In the following, the effects of the parameter errors on the voltage predictive control are analyzed.

Assuming that the actual inductance is L and the modeled one is L_0 , the prediction function in (9) can be rewritten as (11) using the modeled inductance L_0 .

$$\begin{cases}
\mathbf{i}_{f\alpha\beta0}(k+1) = \frac{T_s}{L_0} \left[\mathbf{u}_{\alpha\beta}(k) - \mathbf{u}_{c\alpha\beta}(k) \right] - \frac{T_s}{L_0} \mathbf{i}_{f\alpha\beta}(k) \cdot R_1 \\
+ \mathbf{i}_{f\alpha\beta}(k) \\
\mathbf{u}_{c\alpha\beta0}(k+1) = \frac{T_s}{C} \left[\mathbf{i}_{f\alpha\beta0}(k+1) - \mathbf{i}_{\alpha\beta}(k) \right] + \mathbf{u}_{c\alpha\beta}(k) \\
+ R_2 \left[\mathbf{i}_{f\alpha\beta0}(k+1) - \mathbf{i}_{f\alpha\beta}(k) \right]
\end{cases} (11)$$

Prediction errors, which are the difference between the predicted and actual values deduced based on (9) and (11), are depicted in (12).

$$\begin{cases}
\Delta \boldsymbol{i} = \frac{T_{s}(L-L_{0})}{L_{0}L} \left[\boldsymbol{u}_{\alpha\beta}(k) - \boldsymbol{u}_{c\alpha\beta}(k) - \boldsymbol{i}_{f\alpha\beta}(k) \cdot R_{1} \right] \\
\Delta \boldsymbol{U} = \frac{T_{s}}{C} \left(\boldsymbol{i}_{f\alpha\beta0}(k+1) - \boldsymbol{i}_{f\alpha\beta}(k+1) \right) \\
+ R_{2} \left(\boldsymbol{i}_{f\alpha\beta0}(k+1) - \boldsymbol{i}_{f\alpha\beta}(k+1) \right) \\
= \left(\frac{T_{s}}{C} + R_{2} \right) \Delta \boldsymbol{i}
\end{cases} \tag{12}$$

In the same way, assuming that the actual capacitance is C while the modeled is C_0 , the influence of the

capacitance error on voltage predictive control can also be analyzed as:

$$\Delta U = \frac{T_{\rm s}(C-C0)}{CC0} \left[\mathbf{i}_{\rm f\alpha\beta}(k+1) - \mathbf{i}_{\alpha\beta}(k) \right]$$
 (13)

The analysis of (12) and (13) shows that when the parameter values in the prediction model equal the actual ones in the circuit, i.e., $L\!=\!L_0$ and $C\!=\!C_0$, the current and voltage prediction errors are zero. However, if the parameter values in the prediction model are inconsistent with the actual ones, there will be a voltage prediction error and the optimal switch function selected according to the traditional MPC algorithm will lose its optimality. Consequently, it cannot achieve error-free tracking of the reference values and affects the control performance of the system.

4 Voltage model predictive control with error compensation

4.1 Design of VMPC with error compensation

From the above analysis, it can be seen that when the parameters in the prediction model do not match the actual values, system control performance will deteriorate. In order to reduce the influence of the parameter errors on control performance and improve the voltage control accuracy, a new weighted predictive voltage control method is proposed in this paper. The proposed method uses the weighted sum of the sampled voltage and the predicted one to predict the voltage at the next period, as shown in Fig. 5.

The prediction in (9) can be rewritten using the weighted sum of the sampled voltage and the predicted one considering the weighting factor M, to predict the voltage at the next period, as:

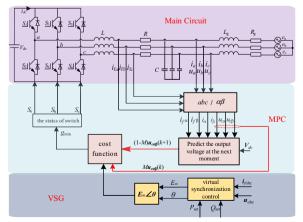


Fig. 5 VSG control block diagram based on the proposed weighted predictive voltage control method

$$\begin{cases} \mathbf{i}_{f\alpha\beta}(k+1) = \frac{T_s}{L} \left[\mathbf{u}_{\alpha\beta}(k) - \mathbf{u}_{c\alpha\beta}(k) \right] - \frac{T_s}{L} \mathbf{i}_{f\alpha\beta}(k) \cdot R_1 \\ + \mathbf{i}_{f\alpha\beta}(k) \\ \mathbf{u}_{c\alpha\beta}(k+1) = (1-M)\mathbf{u}_{c\alpha\beta}(k+1) + M\mathbf{u}_{c\alpha\beta}(k) \\ = (1-M)\frac{T_s}{C} \left[\mathbf{i}_{f\alpha\beta}(k+1) - \mathbf{i}_{\alpha\beta}(k) \right] \\ + (1-M)R_2 \left[\mathbf{i}_{f\alpha\beta}(k+1) - \mathbf{i}_{f\alpha\beta}(k) \right] + \mathbf{u}_{c\alpha\beta}(k) \end{cases}$$

$$(14)$$

4.2 Effectiveness analysis of the proposed weighted VMPC method

The effectiveness of the proposed weighted voltage predictive control method in reducing the influence of parameter changes on the control error is analyzed in this subsection. When the inductance error exists, Eq. (11) can be rewritten as (15) based on (14), while (16) can be obtained from (15) and (9).

$$\begin{cases} \mathbf{i}_{f\alpha\beta0}(k+1) = \frac{T_s}{L_0} \left[\mathbf{u}_{\alpha\beta}(k) - \mathbf{u}_{c\alpha\beta}(k) \right] - \frac{T_s}{L_0} \mathbf{i}_{f\alpha\beta}(k) \cdot R_1 \\ + \mathbf{i}_{f\alpha\beta}(k) \\ \mathbf{u}_{c\alpha\beta0}(k+1) = (1-M)\mathbf{u}_{c\alpha\beta}(k+1) + M\mathbf{u}_{c\alpha\beta}(k) \\ = (1-M)\frac{T_s}{C} \left[\mathbf{i}_{f\alpha\beta0}(k+1) - \mathbf{i}_{\alpha\beta}(k) \right] \\ + (1-M)R_2 \left[\mathbf{i}_{f\alpha\beta0}(k+1) - \mathbf{i}_{f\alpha\beta}(k) \right] + \mathbf{u}_{c\alpha\beta}(k) \end{cases}$$
(15)
$$\begin{cases} \Delta \mathbf{i} = \left(\frac{T_s}{L_0} - \frac{T_s}{L} \right) \left[\mathbf{u}_{\alpha\beta}(k) - \mathbf{u}_{c\alpha\beta}(k) - \mathbf{i}_{f\alpha\beta}(k) \cdot R_1 \right] \\ = \frac{T_s(L-L_0)}{L-L_0} \left[\mathbf{u}_{\alpha\beta}(k) - \mathbf{u}_{c\alpha\beta}(k) - \mathbf{i}_{f\alpha\beta}(k) \cdot R_1 \right] \end{cases}$$

 $\begin{cases}
\Delta \boldsymbol{i} = \left(\frac{T_{s}}{L_{0}} - \frac{T_{s}}{L}\right) \left[\boldsymbol{u}_{\alpha\beta}(k) - \boldsymbol{u}_{c\alpha\beta}(k) - \boldsymbol{i}_{f\alpha\beta}(k) \cdot R_{1}\right] \\
= \frac{T_{s}(L-L_{0})}{L_{0}L} \left[\boldsymbol{u}_{\alpha\beta}(k) - \boldsymbol{u}_{c\alpha\beta}(k) - \boldsymbol{i}_{f\alpha\beta}(k) \cdot R_{1}\right] \\
\Delta \boldsymbol{U} = (1 - M) \frac{T_{s}}{C} \left(\boldsymbol{i}_{f\alpha\beta0}(k+1) - \boldsymbol{i}_{f\alpha\beta}(k+1)\right) \\
+ (1 - M)R_{2} \left(\boldsymbol{i}_{f\alpha\beta0}(k+1) - \boldsymbol{i}_{f\alpha\beta}(k+1)\right) \\
= (1 - M) \left(\frac{T_{s}}{C} + R_{2}\right) \left(\boldsymbol{i}_{f\alpha\beta0}(k+1) - \boldsymbol{i}_{f\alpha\beta}(k+1)\right) \\
= (1 - M) \left(\frac{T_{s}}{C} + R_{2}\right) \Delta \boldsymbol{i}
\end{cases} \tag{16}$

Comparing (16) with (12), if M=1, there is no voltage prediction, while if |1-M|>1, the impact of the inductance error will be further enlarged. However, with |1-M|<1, the voltage prediction error caused by the inductance error can be reduced. Therefore, choosing an appropriate value of M can weaken the influence of the inductance error on voltage tracking and improve voltage control precision.

Similarly, when a capacitance error exists, there are:

$$\begin{cases} \mathbf{i}_{f\alpha\beta}(k+1) = \frac{T_s}{L} \left[\mathbf{u}_{\alpha\beta}(k) - \mathbf{u}_{c\alpha\beta}(k) \right] \\ -\frac{T_s}{L} \mathbf{i}_{f\alpha\beta}(k) \cdot R_1 + \mathbf{i}_{f\alpha\beta}(k) \\ \mathbf{u}_{c\alpha\beta0}(k+1) = (1-M)\mathbf{u}_{c\alpha\beta}(k+1) + M\mathbf{u}_{c\alpha\beta}(k) \\ = (1-M)\frac{T_s}{C_0} \left[\mathbf{i}_{f\alpha\beta}(k+1) - \mathbf{i}_{\alpha\beta}(k) \right] \\ + (1-M)R_2 \left[\mathbf{i}_{f\alpha\beta}(k+1) - \mathbf{i}_{f\alpha\beta}(k) \right] \\ + \mathbf{u}_{c\alpha\beta}(k) \end{cases}$$

$$(17)$$

$$\Delta U = (1 - M) \frac{T_{\rm s}(C - C0)}{CC0} \left[\mathbf{i}_{\rm f\alpha\beta}(k+1) - \mathbf{i}_{\alpha\beta}(k) \right]$$
(18)

Comparing (18) with (13), the same conclusion can be obtained, which means that choosing an M that meets |1-M|<1 can enhance the parameter robustness of the proposed MPC strategy for VSG.

5 Experimental results

To verify the feasibility of the proposed VSG voltage MPC with error compensation, a hardware-in-the-loop experimental platform based on a Typhoon real-time simulator and PE-Expert4 as shown in Fig. 6 is established and studies are conducted. In the experiments, the main circuit of the grid-connected inverter is run in the Typhoon real-time simulator, and the VSG-MPC control algorithm is implemented in the PE-Expert4 (Table 1).

5.1 Comparison with accurate parameters

In order to verify the feasibility of the power outer loop control method with the compensation algorithm, the performance is compared with the traditional control methods without compensation. No parameter mismatch is considered here.

Figure 7 shows the results for the traditional power outer loop without compensation. The active power $P_{\rm ref}$ changes from 500 to 2000 W in Fig. 7a. As can be seen, the actual output active power of the inverter follows the reference change while the reactive power has a small disturbance at the corresponding moment due to the sudden change of the active power. Similar phenomena can be observed during the reactive power $Q_{\rm ref}$ change from 500 to 0 Var in Fig. 7b. In both cases, the actual active and reactive power outputs by the inverter are stabilized at the given values after the transients.

With the same active and reactive power changes, Fig. 8a, b show the experimental results of the power outer loop with the proposed compensation. Comparing Figs. 7 and 8, the results are almost the same, which means that the proposed weighted voltage predictive control method has the same control performance as the conventional method when the parameters are accurate.

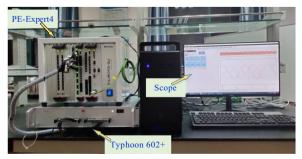


Fig. 6 Typhoon and PE-Expert4 hardware-in-loop experimental platform

Table 1 Simulation parameters

Parameters	Value
DC voltage $V_{\rm dc}/V$	500
Phase voltage of grid e/V	190
Filter inductance L/mH	6.4
Resistance R_1/Ω	0.1
Filter capacitor C/mF	0.6
Resistance R_2/Ω	0.1
Grid-side inductance Lg/mH	1
Grid-side resistance Rg/Ω	1.5
Switching frequency f _s /kHz	40
Grid frequency f/Hz	50
Droop coefficient D_q	0.05
Moment of Inertia J/kg m ²	0.0000005
Damping coefficient D_p	0.0003
Weight factor M	0.7

Figures 9 and 10 further show the results during a sudden change of active power without and with error compensation, respectively. Figures 9a and 10a show the complete change process of the active power, while Figs. 9b, c and 10b, c show the details of the β -axis voltage changes in different time ranges during the transients. As can be seen, for both cases, when the active power changes suddenly from 500 to 2000 W, the β -axis voltage values are increased. Comparing Figs. 9 and 10, it can be seen that the waveforms corresponding to the two methods are almost identical. Both methods produce satisfactory voltage waveforms and the differences between the actual and the reference β -axis voltages for the two

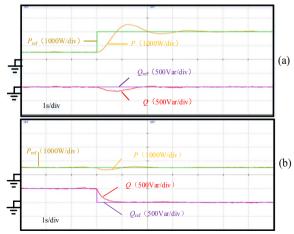


Fig. 7 Experimental waveforms of the power outer loop without compensation. **a** Active power $P_{\rm ref}$ changes from 500 to 2000 W. **b** Reactive power $Q_{\rm ref}$ changes from 500 to 0 Var

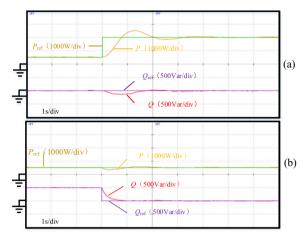


Fig. 8 Experimental waveforms of the power outer loop with compensation. (a) Active power $P_{\rm ref}$ changes from 500 to 2000 W. (b) Reactive power $Q_{\rm ref}$ changes from 500 to 0Var

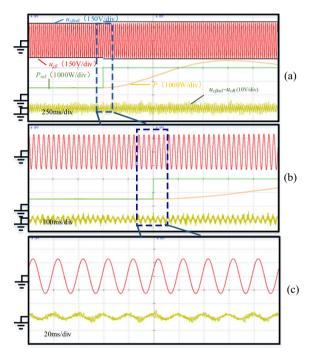


Fig. 9 Experimental waveforms during sudden change of active power without error compensation. **a** 250 ms/div. **b** 100 ms/div. **c** 20 ms/div

methods are almost identical in both dynamic and steady states.

Similarly, further experimental waveforms during reactive power change for the two methods are compared in Figs. 11 and 12. As seen there, when the reactive power changes suddenly from 500 to 0 Var, the β -axis voltage values are reduced, while the waveforms corresponding to the two methods are almost identical.

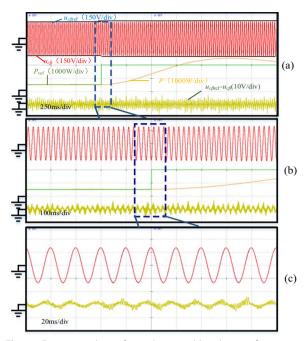


Fig. 10 Experimental waveforms during sudden change of active power with error compensation. **a** 250 ms/div. **b** 100 ms/div. **c** 20 ms/div.

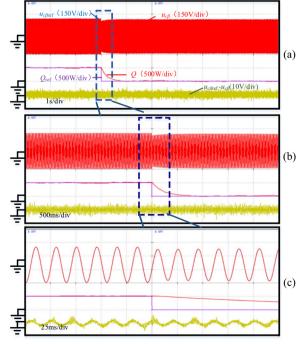


Fig. 11 Experimental waveforms during sudden change of reactive power without error compensation. **a** 1 s/div. **b** 500 ms/div. **c** 25 ms/div

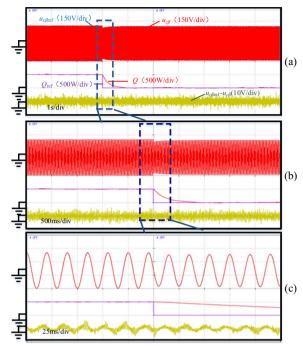


Fig. 12 Experimental waveforms during sudden change of reactive power with error compensation. **a** 1 s/div. **b** 500 ms/div. **c** 25 ms/div

In summary, the power outer loop with the proposed compensation algorithm can achieve the same control effect as the conventional power outer loop without compensation.

5.2 Comparison with inaccurate parameters

To verify that the compensation strategy can reduce the influence of model errors on system control performance, the following experiments are carried out. The reference active power $P_{\rm ref}$ is set to 500 W, while the reference reactive power $Q_{\rm ref}$ is 0 Var.

Figure 13a shows the results during the sudden change of parameters. The modeled inductance and capacitance become 1/3 of the actual values at time t_1 . As is shown, the difference between the actual and reference β -axis voltage values becomes larger after the changes of the inductance and capacitance values. Figure 13b shows a comparison of the two strategies with inaccurate parameters. M=0 means there is no compensation for the voltage prediction value, while M=0.7 means there is an error compensation for the voltage prediction value. As can be seen, the difference between the actual and reference β -axis voltage values under M=0.7 is much smaller than the one under M=0.

Therefore, choosing an appropriate value of M can weaken the influence of the parameter error on voltage tracking, enhance the robustness in the face of parameter changes, and improve voltage control precision.

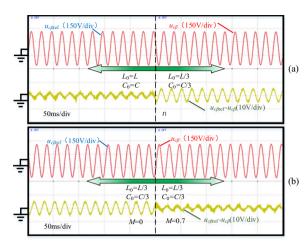


Fig. 13 a Experimental results during sudden change of parameters. **b** Comparison of the two strategies

With the same inductance and capacitance errors, Figs. 14 and 15 show the results during a sudden change of active power from 500 to 2000 W, without and with error compensation, respectively. Figures 14a and 15a

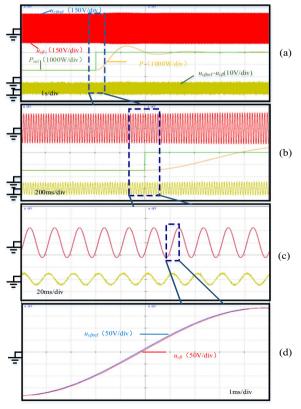


Fig. 14 Experimental waveforms during sudden change of active power without error compensation. **a** 1 s/div. **b** 200 ms/div. **c** 20 ms/div. **d** 1 ms/div

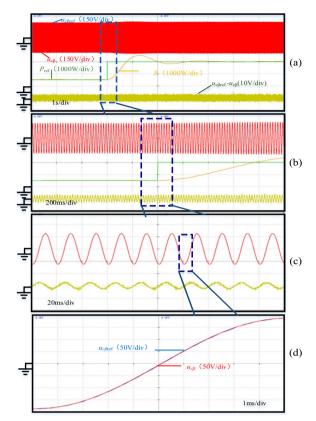


Fig. 15 Experimental waveforms during sudden change of active power with error compensation. **a** 1 s/div. **b** 200 ms/div. **c** 20 ms/div. **d** 1 ms/div

show the complete change process during the sudden change of active power, while Figs. 14b-d and 15b-d show the details of the β -axis voltage changes in different time ranges during the transients.

Comparing the steady-state differences between the actual and reference $\beta\text{-axis}$ voltage before and after the sudden active power change in Figs. 14a and 15a, it can be seen that the compensation strategy can significantly reduce the voltage deviation and $\beta\text{-axis}$ voltage error in steady state. In addition, by comparing Figs. 14d and 15d, it becomes apparent that the compensation strategy can minimize the voltage error caused by parameter errors, and achieve better tracking of the reference voltage in the dynamic process.

Similarly, Figs. 16 and 17 are the experimental waveforms for the two control methods when the reactive power changes from 500 to 0 Var. Again, it can be seen that the compensation strategy can significantly reduce the voltage errors caused by parameter mismatch in both steady state and in transient during a reactive power step change.

In summary, the proposed compensation strategy can reduce the influence of model errors on system control

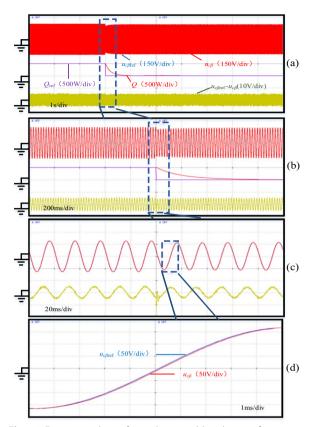


Fig. 16 Experimental waveforms during sudden change of reactive power without error compensation. **a** 1 s/div. **b** 200 ms/div. **c** 20 ms/div. **d** 1 ms/div

performance, enhance the robustness against parameter variation in both the steady state and dynamic process.

6 Conclusion

A new MPC method to control the output voltage of the VSG is proposed in this paper, one with enhanced robustness against parameter variation. The important conclusions can be summarized as follows:

- (1) When the parameters are perfectly matched, the proposed control strategy with compensation is almost identical to the traditional control strategy in both static and dynamic process, and both have excellent control performance.
- (2) When the parameters are not matched, the predicted voltage error of the conventional MPC method will increase significantly due to its sensitivity to parameter changes.
- (3) In contrast, with parameter mismatch, the proposed weighted predictive capacitor voltage control method can reduce the influence of parameter changes and improve the parameter robustness both in the steady and dynamic state.

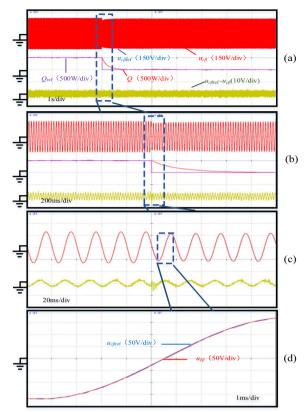


Fig. 17 Experimental waveforms during sudden change of reactive power with error compensation. **a** 1 s/div. **b** 200 ms/div. **c** 20 ms/div. **d** 1 ms/div

Finally, the effectiveness of the proposed method is verified through theoretical analysis, and its feasibility and superiority are further demonstrated through control hardware-in-the-loop experimental tests.

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Authors' contributions

LLG proposed the methodological framework and mathematical model, ZYX carried out theoretical analysis of the process and performed simulation and experiment to verify the proposed method. NJ, YYL and WW offered help in theory and practice, read and put forward suggestions for the paper. All authors read and approved the final manuscript.

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Availability of data and materials

Not applicable.

Declaration

Competing interests

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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